

2017 Yazokulu BLNT6NBS Dersnotu

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2017 Yazokulu Vize-Quiz-Final

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## 2017 Yaz Okulu QUIZ1

**Soru**  $y(n) = x(-2n)$  zamanla değişip değişmediğiniz ispatlayınız?

### Çözüm

$$x_1(n) = x(n - k)$$

$$\left. \begin{aligned} y_1(n) &= T[x_1(n)] = x_1(-2n) = x(-2n - k) \\ y(n - k) &= x(-2(n - k)) = x(-2n + 2k) \end{aligned} \right\} \text{eşit olmadığı için zamanla değişir}$$

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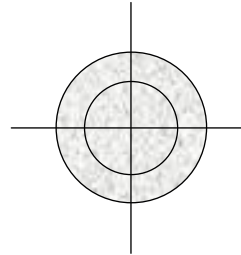
**Soru** DZD bir sistemin  $H(z) = \frac{z^{-1}}{1 - \frac{1}{4}z^{-2}}$

- a) Sistemin kararlı olması için gerekli YB=?
- b) Sistemin kararlı  $h(n) = ?$
- c) Sistemin nedensel olup olmadığını gösteriniz

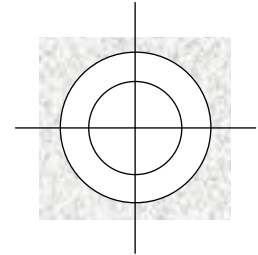
$$|z| > \frac{1}{2}$$

**Çözüm**

$$H(z) = \frac{z^{-1}}{1 - \frac{1}{4}z^{-2}} = \frac{z^{-1}}{\left(1 - \frac{1}{2}z^{-1}\right)\left(1 + \frac{1}{2}z^{-1}\right)}$$



Nedensel değil  
(Çemberin içi)



Nedensel  
(Çemberin dışı)

$$H(z) = \frac{A}{\underbrace{\left(1 - \frac{1}{2}z^{-1}\right)}_{|z| > \frac{1}{2}}} + \frac{B}{\underbrace{\left(1 + \frac{1}{2}z^{-1}\right)}_{|z| < \frac{1}{2}}}$$

$$A = \frac{z^{-1}}{1 + \frac{1}{2z^{-1}}}\bigg|_{z^{-1}=2} = 1$$

$$B = \frac{z^{-1}}{1 - \frac{1}{2z^{-1}}}\bigg|_{z^{-1}=-2} = -1$$

$$H(z) = \frac{1}{\left(1 - \frac{1}{2}z^{-1}\right)} - \frac{1}{\left(1 + \frac{1}{2}z^{-1}\right)}$$

YB  $|z| > \frac{1}{2}$

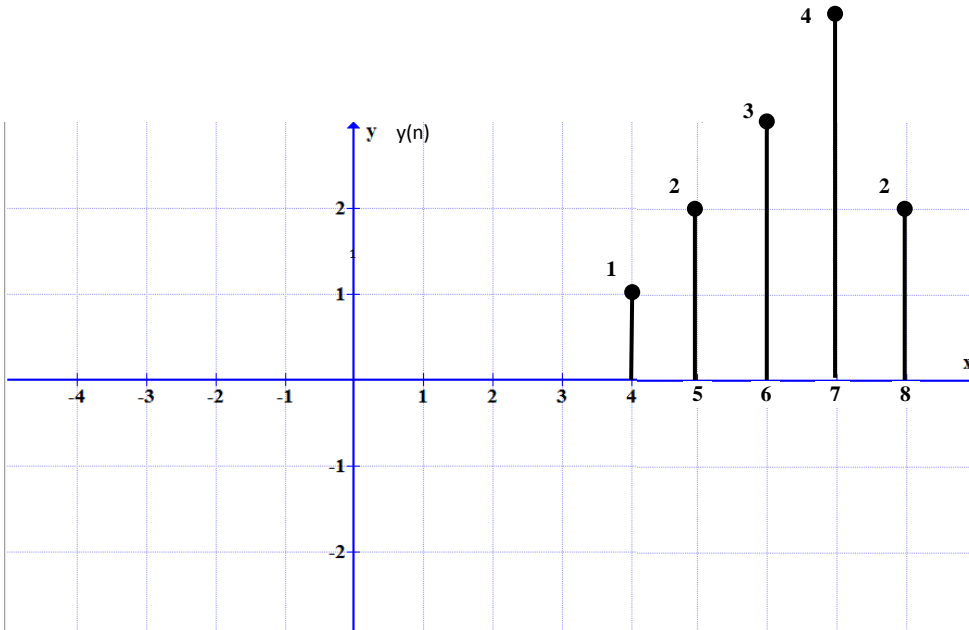
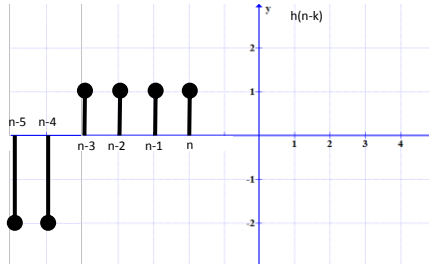
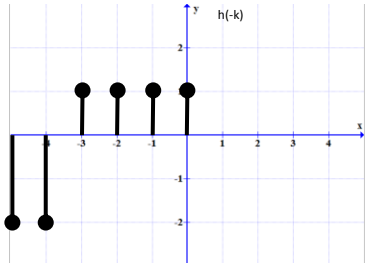
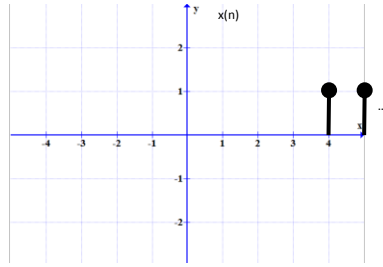
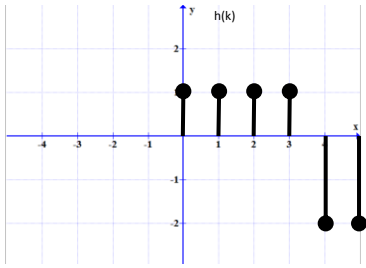
Çemberin dışı

Nedensel

$$h(n) = \left(\frac{1}{2}\right)^n u(n) - \left(-\frac{1}{2}\right)^n u(n)$$

**Soru1 (30P)**  $h(n) = \begin{cases} 0 & n < 0 \\ 1 & 0 \leq n \leq 3 \\ -2 & 4 \leq n \leq 5 \\ 0 & n > 5 \end{cases}$   $x(n) = u(n-4)$   $y(n)$  'i çiziniz?

**Çözüm**



$n < 4$	$y(n) = 0$
$n = 4$	$y(4) = 1$
$n = 5$	$y(5) = 2$
$n = 6$	$y(6) = 3$
$n = 7$	$y(7) = 4$
$n = 8$	$y(8) = 2$
$n = 9$	$y(9) = 0$
$n > 9$	$y(n) = 0$

**Soru2 (35P)**  $y(n) - y(n-1) = x(n) + \frac{1}{2}x(n-1)$      $y(-1) = \frac{1}{2}$      $x(n) = (-1)^n u(n)$      $y_i(n) = ?$

**Çözüm**

$$\begin{array}{l}
 y_d = c_1 \lambda^n \\
 y_d = \frac{1}{2}(1)^n
 \end{array}
 \quad
 \begin{array}{l}
 y(n) = \lambda^n \\
 y(n) - y(n-1) = x(n) + \frac{1}{2}x(n-1) \\
 \lambda^n - \lambda^{n-1} = 0 \\
 \lambda^{n-1}(\lambda - 1) = 0 \\
 \underbrace{\hspace{2cm}}_0 \\
 \lambda = 1
 \end{array}
 \quad
 n=0 \left\{ \begin{array}{l}
 y(n) - y(n-1) = 0 \\
 y(0) - y(-1) = 0 \\
 y(0) - \frac{1}{2} = 0 \\
 y(0) = \frac{1}{2} \\
 c_1 = \frac{1}{2}
 \end{array} \right.$$

$$\begin{array}{l}
 x(n) = (-1)^n u(n) \\
 y_{\delta}(n) = K(-1)^n u(n) \\
 y_{\delta}(n) = \frac{1}{4}(-1)^n u(n)
 \end{array}
 \quad
 \begin{array}{l}
 y(n) - y(n-1) = x(n) + \frac{1}{2}x(n-1) \\
 K(-1)u(n) - K(-1)^{n-1}u(n-1) = (-1)^n u(n) + \frac{1}{2}(-1)^{n-1}u(n-1) \\
 (-1)^{n-1}(-K - K) = (-1)^{n-1}\left(-1 + \frac{1}{2}\right) \\
 -2K = -\frac{1}{2} \\
 K = \frac{1}{4}
 \end{array}$$

$$\begin{array}{l}
 y_z(n) = c_2(1)^n + y_{\delta}(n) \\
 y_z(n) = c_2(1)^n + \frac{1}{4}(-1)^n u(n) \\
 y_z(n) = \frac{3}{4}(1)^n + \frac{1}{4}(-1)^n u(n)
 \end{array}
 \quad
 n=0 \left\{ \begin{array}{l}
 y(n) - y(n-1) = x(n) + \frac{1}{2}x(n-1) \\
 y(0) - \cancel{y(-1)} = x(0) + \frac{1}{2}\cancel{x(-1)} \\
 \underbrace{\hspace{2cm}}_0 \qquad \underbrace{\hspace{2cm}}_0 \\
 y(0) = 1
 \end{array} \right.
 \quad
 \begin{array}{l}
 c_2(1)^n + \frac{1}{4}(-1)^n u(n) \\
 c_2(1)^0 + \frac{1}{4}(-1)^0 u(0) \\
 c_2 + \frac{1}{4} = y(0) = 1 \\
 c_2 = \frac{3}{4}
 \end{array}$$

$$\begin{aligned}
 y_i(n) &= y_d(n) + y_{\delta}(n) \\
 &= \frac{1}{2}(1)^n + \frac{3}{4}(1)^n + \frac{1}{4}(-1)^n u(n) \\
 &= \left( \frac{5}{4} + \frac{1}{4}(-1)^n \right) u(n)
 \end{aligned}$$

**2017 Yaz Okulu VİZE**

**Soru3 (35P)**  $x(n) = \left(\frac{1}{2}\right)^n u(n)$       $x_1(n) = nx(-n+2)$       $X_1(z) = ?$       $YB = ?$

$$x(n) = \left(\frac{1}{2}\right)^n u(n)$$

$$X(z) = \frac{1}{1 - \frac{1}{2}z^{-1}} \quad |z| > \frac{1}{2}$$

$$x_2(n) = x(n+2)$$

$$X_2(z) = z^2 \frac{1}{1 - \frac{1}{2}z^{-1}} \quad |z| > \frac{1}{2}$$

$$x_3(n) = x_2(-n)$$

$$x_2(-n) = x(-n+2)$$

$$X_3(z) = X_2(z^{-1})$$

$$X_3(z) = (z^{-1})^2 \frac{1}{1 - \frac{1}{2}(z^{-1})^{-1}} \quad |z| > \frac{1}{2}$$

$$X_3(z) = z^{-2} \frac{1}{1 - \frac{1}{2}z}$$

$$x_1(n) = nx_3(n)$$

$$X_1(z) = -z \frac{d}{dz} X_3(z)$$

$$= -z \frac{d}{dz} \frac{z^{-2}}{1 - \frac{1}{2}z}$$

$$= -z \frac{-2z^{-3} \left(1 - \frac{1}{2}z\right) + \frac{1}{2}z^{-2}}{\left(1 - \frac{1}{2}z\right)^2} \quad |z| < 2$$

